

Blog Entry © Wednesday, October 29, 2025, by James Pate Williams, Jr. Hydrogenic Atomic Spectral Lines

Formulas:

$$E = h\nu = -13.6Z^2 \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right) (\text{units: eV})$$

$$\nu = \frac{E}{h} (\text{units: Hz})$$

$$\lambda = \frac{c}{\nu} (\text{units: } 10^{-10} \text{ m} = \text{Angstrom})$$

HydrogenSpectralLines

File Help

Series:

Brackett n1 = 4 n2 >= 5

n2:

8

atom:

hydrogen

formula:

energy eV

Compute

Cancel

Clear

| | | | | | |
|----------|----------|-----------|---|---|------------|
| Lyman | hydrogen | energy eV | 1 | 2 | -10.200000 |
| Lyman | hydrogen | energy eV | 1 | 3 | -12.088889 |
| Lyman | hydrogen | energy eV | 1 | 4 | -12.750000 |
| Lyman | hydrogen | energy eV | 1 | 5 | -13.056000 |
| Balmer | hydrogen | energy eV | 2 | 3 | -1.888889 |
| Balmer | hydrogen | energy eV | 2 | 4 | -2.550000 |
| Balmer | hydrogen | energy eV | 2 | 5 | -2.856000 |
| Balmer | hydrogen | energy eV | 2 | 6 | -3.022222 |
| Paschen | hydrogen | energy eV | 3 | 4 | -0.661111 |
| Paschen | hydrogen | energy eV | 3 | 5 | -0.967111 |
| Paschen | hydrogen | energy eV | 3 | 6 | -1.133333 |
| Paschen | hydrogen | energy eV | 3 | 7 | -1.233560 |
| Brackett | hydrogen | energy eV | 4 | 5 | -0.306000 |
| Brackett | hydrogen | energy eV | 4 | 6 | -0.472222 |
| Brackett | hydrogen | energy eV | 4 | 7 | -0.572449 |
| Brackett | hydrogen | energy eV | 4 | 8 | -0.637500 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: hydrogen

formula: frequency Hz

Compute

Cancel

Clear

| | | | | | |
|----------|----------|--------------|---|---|--------------------------|
| Lyman | hydrogen | frequency Hz | 1 | 2 | -2466349027477569.000000 |
| Lyman | hydrogen | frequency Hz | 1 | 3 | -2923080328862304.000000 |
| Lyman | hydrogen | frequency Hz | 1 | 4 | -3082936284346961.500000 |
| Lyman | hydrogen | frequency Hz | 1 | 5 | -3156926755171288.500000 |
| Balmer | hydrogen | frequency Hz | 2 | 3 | -456731301384735.000000 |
| Balmer | hydrogen | frequency Hz | 2 | 4 | -616587256869392.250000 |
| Balmer | hydrogen | frequency Hz | 2 | 5 | -690577727693719.375000 |
| Balmer | hydrogen | frequency Hz | 2 | 6 | -730770082215576.000000 |
| Paschen | hydrogen | frequency Hz | 3 | 4 | -159855955484657.218750 |
| Paschen | hydrogen | frequency Hz | 3 | 5 | -233846426308984.281250 |
| Paschen | hydrogen | frequency Hz | 3 | 6 | -274038780830841.000000 |
| Paschen | hydrogen | frequency Hz | 3 | 7 | -298273502945133.062500 |
| Brackett | hydrogen | frequency Hz | 4 | 5 | -73990470824327.078125 |
| Brackett | hydrogen | frequency Hz | 4 | 6 | -114182825346183.750000 |
| Brackett | hydrogen | frequency Hz | 4 | 7 | -138417547460475.843750 |
| Brackett | hydrogen | frequency Hz | 4 | 8 | -154146814217348.062500 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: hydrogen

formula: wavelength A

Compute

Cancel

Clear

| | | | | | |
|----------|----------|--------------|---|---|---------------|
| Lyman | hydrogen | wavelength A | 1 | 2 | -1215.531357 |
| Lyman | hydrogen | wavelength A | 1 | 3 | -1025.604582 |
| Lyman | hydrogen | wavelength A | 1 | 4 | -972.425086 |
| Lyman | hydrogen | wavelength A | 1 | 5 | -949.633873 |
| Balmer | hydrogen | wavelength A | 2 | 3 | -6563.869327 |
| Balmer | hydrogen | wavelength A | 2 | 4 | -4862.125428 |
| Balmer | hydrogen | wavelength A | 2 | 5 | -4341.183418 |
| Balmer | hydrogen | wavelength A | 2 | 6 | -4102.418330 |
| Paschen | hydrogen | wavelength A | 3 | 4 | -18753.912364 |
| Paschen | hydrogen | wavelength A | 3 | 5 | -12820.057280 |
| Paschen | hydrogen | wavelength A | 3 | 6 | -10939.782212 |
| Paschen | hydrogen | wavelength A | 3 | 7 | -10050.924908 |
| Brackett | hydrogen | wavelength A | 4 | 5 | -40517.711897 |
| Brackett | hydrogen | wavelength A | 4 | 6 | -26255.477309 |
| Brackett | hydrogen | wavelength A | 4 | 7 | -21658.558723 |
| Brackett | hydrogen | wavelength A | 4 | 8 | -19448.501711 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: helium+

formula: energy eV

Compute

Cancel

Clear

| | | | | | |
|----------|---------|-----------|---|---|------------|
| Lyman | helium+ | energy eV | 1 | 2 | -40.800000 |
| Lyman | helium+ | energy eV | 1 | 3 | -48.355556 |
| Lyman | helium+ | energy eV | 1 | 4 | -51.000000 |
| Lyman | helium+ | energy eV | 1 | 5 | -52.224000 |
| Balmer | helium+ | energy eV | 2 | 3 | -7.555556 |
| Balmer | helium+ | energy eV | 2 | 4 | -10.200000 |
| Balmer | helium+ | energy eV | 2 | 5 | -11.424000 |
| Balmer | helium+ | energy eV | 2 | 6 | -12.088889 |
| Paschen | helium+ | energy eV | 3 | 4 | -2.644444 |
| Paschen | helium+ | energy eV | 3 | 5 | -3.868444 |
| Paschen | helium+ | energy eV | 3 | 6 | -4.533333 |
| Paschen | helium+ | energy eV | 3 | 7 | -4.934240 |
| Brackett | helium+ | energy eV | 4 | 5 | -1.224000 |
| Brackett | helium+ | energy eV | 4 | 6 | -1.888889 |
| Brackett | helium+ | energy eV | 4 | 7 | -2.289796 |
| Brackett | helium+ | energy eV | 4 | 8 | -2.550000 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: helium+

formula: frequency Hz

Compute

Cancel

Clear

| | | | | | |
|----------|---------|--------------|---|---|---------------------------|
| Lyman | helium+ | frequency Hz | 1 | 2 | -9865396109910276.000000 |
| Lyman | helium+ | frequency Hz | 1 | 3 | -11692321315449216.000000 |
| Lyman | helium+ | frequency Hz | 1 | 4 | -12331745137387846.000000 |
| Lyman | helium+ | frequency Hz | 1 | 5 | -12627707020685154.000000 |
| Balmer | helium+ | frequency Hz | 2 | 3 | -1826925205538940.000000 |
| Balmer | helium+ | frequency Hz | 2 | 4 | -2466349027477569.000000 |
| Balmer | helium+ | frequency Hz | 2 | 5 | -2762310910774877.500000 |
| Balmer | helium+ | frequency Hz | 2 | 6 | -2923080328862304.000000 |
| Paschen | helium+ | frequency Hz | 3 | 4 | -639423821938628.875000 |
| Paschen | helium+ | frequency Hz | 3 | 5 | -935385705235937.125000 |
| Paschen | helium+ | frequency Hz | 3 | 6 | -1096155123323364.000000 |
| Paschen | helium+ | frequency Hz | 3 | 7 | -1193094011780532.250000 |
| Brackett | helium+ | frequency Hz | 4 | 5 | -295961883297308.312500 |
| Brackett | helium+ | frequency Hz | 4 | 6 | -456731301384735.000000 |
| Brackett | helium+ | frequency Hz | 4 | 7 | -553670189841903.375000 |
| Brackett | helium+ | frequency Hz | 4 | 8 | -616587256869392.250000 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: helium+

formula: wavelength A

Compute

Cancel

Clear

| | | | | | |
|----------|---------|--------------|---|---|---------------|
| Lyman | helium+ | wavelength A | 1 | 2 | -303.882839 |
| Lyman | helium+ | wavelength A | 1 | 3 | -256.401146 |
| Lyman | helium+ | wavelength A | 1 | 4 | -243.106271 |
| Lyman | helium+ | wavelength A | 1 | 5 | -237.408468 |
| Balmer | helium+ | wavelength A | 2 | 3 | -1640.967332 |
| Balmer | helium+ | wavelength A | 2 | 4 | -1215.531357 |
| Balmer | helium+ | wavelength A | 2 | 5 | -1085.295854 |
| Balmer | helium+ | wavelength A | 2 | 6 | -1025.604582 |
| Paschen | helium+ | wavelength A | 3 | 4 | -4688.478091 |
| Paschen | helium+ | wavelength A | 3 | 5 | -3205.014320 |
| Paschen | helium+ | wavelength A | 3 | 6 | -2734.945553 |
| Paschen | helium+ | wavelength A | 3 | 7 | -2512.731227 |
| Brackett | helium+ | wavelength A | 4 | 5 | -10129.427974 |
| Brackett | helium+ | wavelength A | 4 | 6 | -6563.869327 |
| Brackett | helium+ | wavelength A | 4 | 7 | -5414.639681 |
| Brackett | helium+ | wavelength A | 4 | 8 | -4862.125428 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: helium+

formula: wavelength A

Compute

Cancel

Clear

| | | | | | |
|----------|---------|--------------|---|---|---------------|
| Lyman | helium+ | wavelength A | 1 | 2 | -303.882839 |
| Lyman | helium+ | wavelength A | 1 | 3 | -256.401146 |
| Lyman | helium+ | wavelength A | 1 | 4 | -243.106271 |
| Lyman | helium+ | wavelength A | 1 | 5 | -237.408468 |
| Balmer | helium+ | wavelength A | 2 | 3 | -1640.967332 |
| Balmer | helium+ | wavelength A | 2 | 4 | -1215.531357 |
| Balmer | helium+ | wavelength A | 2 | 5 | -1085.295854 |
| Balmer | helium+ | wavelength A | 2 | 6 | -1025.604582 |
| Paschen | helium+ | wavelength A | 3 | 4 | -4688.478091 |
| Paschen | helium+ | wavelength A | 3 | 5 | -3205.014320 |
| Paschen | helium+ | wavelength A | 3 | 6 | -2734.945553 |
| Paschen | helium+ | wavelength A | 3 | 7 | -2512.731227 |
| Brackett | helium+ | wavelength A | 4 | 5 | -10129.427974 |
| Brackett | helium+ | wavelength A | 4 | 6 | -6563.869327 |
| Brackett | helium+ | wavelength A | 4 | 7 | -5414.639681 |
| Brackett | helium+ | wavelength A | 4 | 8 | -4862.125428 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: lithium++

formula: frequency Hz

Compute

Cancel

Clear

| | | | | | |
|----------|-----------|--------------|---|---|---------------------------|
| Lyman | lithium++ | frequency Hz | 1 | 2 | -22197141247298120.000000 |
| Lyman | lithium++ | frequency Hz | 1 | 3 | -26307722959760732.000000 |
| Lyman | lithium++ | frequency Hz | 1 | 4 | -27746426559122648.000000 |
| Lyman | lithium++ | frequency Hz | 1 | 5 | -28412340796541596.000000 |
| Balmer | lithium++ | frequency Hz | 2 | 3 | -4110581712462615.500000 |
| Balmer | lithium++ | frequency Hz | 2 | 4 | -5549285311824530.000000 |
| Balmer | lithium++ | frequency Hz | 2 | 5 | -6215199549243474.000000 |
| Balmer | lithium++ | frequency Hz | 2 | 6 | -6576930739940183.000000 |
| Paschen | lithium++ | frequency Hz | 3 | 4 | -1438703599361915.000000 |
| Paschen | lithium++ | frequency Hz | 3 | 5 | -2104617836780858.250000 |
| Paschen | lithium++ | frequency Hz | 3 | 6 | -2466349027477569.000000 |
| Paschen | lithium++ | frequency Hz | 3 | 7 | -2684461526506197.500000 |
| Brackett | lithium++ | frequency Hz | 4 | 5 | -665914237418943.625000 |
| Brackett | lithium++ | frequency Hz | 4 | 6 | -1027645428115653.875000 |
| Brackett | lithium++ | frequency Hz | 4 | 7 | -1245757927144282.500000 |
| Brackett | lithium++ | frequency Hz | 4 | 8 | -1387321327956132.500000 |

HydrogenSpectralLines

File Help

Series: Brackett n1 = 4 n2 >= 5

n2: 8

atom: lithium++

formula: wavelength A

Compute

Cancel

Clear

| | | | | | |
|----------|-----------|--------------|---|---|--------------|
| Lyman | lithium++ | wavelength A | 1 | 2 | -135.059040 |
| Lyman | lithium++ | wavelength A | 1 | 3 | -113.956065 |
| Lyman | lithium++ | wavelength A | 1 | 4 | -108.047232 |
| Lyman | lithium++ | wavelength A | 1 | 5 | -105.514875 |
| Balmer | lithium++ | wavelength A | 2 | 3 | -729.318814 |
| Balmer | lithium++ | wavelength A | 2 | 4 | -540.236159 |
| Balmer | lithium++ | wavelength A | 2 | 5 | -482.353713 |
| Balmer | lithium++ | wavelength A | 2 | 6 | -455.824259 |
| Paschen | lithium++ | wavelength A | 3 | 4 | -2083.768040 |
| Paschen | lithium++ | wavelength A | 3 | 5 | -1424.450809 |
| Paschen | lithium++ | wavelength A | 3 | 6 | -1215.531357 |
| Paschen | lithium++ | wavelength A | 3 | 7 | -1116.769434 |
| Brackett | lithium++ | wavelength A | 4 | 5 | -4501.967989 |
| Brackett | lithium++ | wavelength A | 4 | 6 | -2917.275257 |
| Brackett | lithium++ | wavelength A | 4 | 7 | -2406.506525 |
| Brackett | lithium++ | wavelength A | 4 | 8 | -2160.944635 |

